

## Motion

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1. Three different processes that can occur in an ideal monoatomic gas are shown in the $P$ vs $V$ diagram. The paths are labelled as $A \rightarrow B, A \rightarrow C$ and $A \rightarrow D$. The change in internal energies during these process are taken as $\mathrm{E}_{\mathrm{AB}}, \mathrm{E}_{\mathrm{AC}}$ and $\mathrm{E}_{\mathrm{AD}}$ and the workdone as $\mathrm{W}_{\mathrm{AB}}, \mathrm{W}_{\mathrm{AC}}$ and $\mathrm{E}_{\mathrm{AD}}$. The correct relation between these parameters are :

(1) $\mathrm{E}_{\mathrm{AB}}=\mathrm{E}_{\mathrm{AC}}<\mathrm{E}_{\mathrm{AD}}, \mathrm{W}_{\mathrm{AB}}>0, \mathrm{~W}_{\mathrm{AC}}=0, \mathrm{~W}_{\mathrm{AD}}<0$
(2) $\mathrm{E}_{\mathrm{AB}}>\mathrm{E}_{\mathrm{AC}}>\mathrm{E}_{\mathrm{AD}}, W_{\mathrm{AB}}<\mathrm{W}_{\mathrm{AC}}<\mathrm{W}_{\mathrm{AD}}$
(3) $E_{A B}<E_{A C}<E_{A D}, W_{A B}>0, W_{A C}>W_{A D}$
(4) $E_{A B}^{A B}=E_{A C}^{A C}=E_{A D}^{A D}, W_{A B}^{A B}>0, W_{A C}^{A C}=0, W_{A D}>0$

Sol. 1 (Bonus)
$E_{A B}=E_{A C}=E_{A D}$
$d U=\frac{n f R}{2}\left(T_{f}-T_{i}\right)$
$\mathrm{w}_{\mathrm{AB}}>0(+) \mathrm{V} \uparrow$
$\mathrm{w}_{\mathrm{AC}}=0 \mathrm{~V}$ const.
$\mathrm{w}_{\mathrm{AD}}<0(-) \mathrm{V} \downarrow$

2. With increasing biasing voltage of a photodiode, the photocurrent magnitude :
(1) increases initially and saturates finally
(2) remains constant
(3) increases linearly
(4) increases initially and after attaining certain value, it decreases

Sol. 1
By theory

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3. A square loop of side $2 a$, and carrying current $I$, is kept in $X Z$ plane with its centre at origin. A long wire carrying the same current $I$ is placed parallel to the $z$-axis and passing through the point $(0, b$, $0),(b \gg a)$. The magnitude of the torque on the loop about $z$-axis is given by :
(1) $\frac{2 \mu_{0} I^{2} a^{3}}{\pi b^{2}}$
(2) $\frac{\mu_{0} I^{2} a^{3}}{2 \pi b^{2}}$
(3) $\frac{2 \mu_{0} I^{2} a^{2}}{\pi b}$
(4) $\frac{\mu_{0} I^{2} a^{2}}{2 \pi b}$

## Sol. 3


$M=I_{2}(2 a)^{2}=4 a^{2} I_{2}$
(magnetic moment)
$B=\frac{\mu_{0} I_{2}}{2 \pi b}$
$\tau=M B \sin \theta$

$\theta$ angle between $B$ and $M\left[\theta=90^{\circ}\right]$
$\tau=4\left(a^{2} I_{2}\right) \frac{\mu_{0} I_{1}}{2 \pi b}$
$\tau=\frac{2 \mu_{0} \mathrm{I}_{1} \mathrm{I}_{2} \mathrm{a}^{2}}{\pi \mathrm{~b}}=\frac{2 \mu_{0} \mathrm{I}^{2} \mathrm{a}^{2}}{\pi \mathrm{~b}}$

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4. Assume that the displacement (s) of air is proportional to the pressure difference ( $\Delta \mathrm{p}$ ) created by a sound wave. Displacement(s) further depends on the speed of sound (v), density of air ( $\rho$ ) and the frequency (f). If $\Delta \mathrm{p} \sim 10 \mathrm{~Pa}, v \sim 300 \mathrm{~m} / \mathrm{s}, \rho \sim 1 \mathrm{~kg} / \mathrm{m}^{3}$ and $\mathrm{f} \sim 1000 \mathrm{~Hz}$, then s will be of the order of (take the multiplicative constant to be 1)
(1) 1 mm
(2) 10 mm
(3) $\frac{1}{10} \mathrm{~mm}$
(4) $\frac{3}{100} \mathrm{~mm}$

Ans. 4
$S_{0}=\frac{\Delta P}{\beta k}=\frac{\Delta P}{\rho v^{2} \frac{\omega}{v}}=\frac{\Delta P}{\rho v \omega}=\frac{\Delta P}{\rho v 2 \pi f}$
$\therefore$ Proportionally constant $=1$

$$
\begin{aligned}
S_{0} \quad & =\frac{\Delta \mathrm{P}}{\rho \mathrm{vf}} \\
& =\frac{10}{1 \times 300 \times 1000} \mathrm{~m} \\
& =\frac{10}{300} \mathrm{~mm} \\
& =\frac{3}{90} \\
& \simeq \frac{3}{100} \mathrm{~mm}
\end{aligned}
$$

5. Two capacitors of capacitances $C$ and $2 C$ are charged to potential differences $V$ and $2 V$, respectively. These are then connected in parallel in such a manner that the positive terminal of one is connected to the negative terminal of the other. The final energy of this configuration is :
(1) zero
(2) $\frac{9}{2} \mathrm{CV}^{2}$
(3) $\frac{25}{6} \mathrm{CV}^{2}$
(4) $\frac{3}{2} \mathrm{CV}^{2}$

Sol. 4


$$
U_{i}=\frac{1}{2} C v^{2}+\frac{1}{2}(2 C)(2 v)^{2}
$$



$$
=\frac{9}{2} C v^{2}
$$

$$
\mathrm{q}_{1}+\mathrm{q}_{2}=\mathrm{q}_{1}^{\prime}+\mathrm{q}_{2}^{\prime}
$$

$$
-\mathrm{CV}+\left(2 \mathrm{C}(2 \mathrm{~V})=(\mathrm{C}+2 \mathrm{C}) \mathrm{V}^{\prime}\right.
$$

$$
V^{\prime}=\frac{3 C V}{3 C}=V
$$

$\mathrm{U}_{\mathrm{f}}=\frac{1}{2} C V^{2}+\frac{1}{2}(2 C) \mathrm{V}^{2}$
$U_{f}=\frac{3}{2} C V^{2}$

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6. A helicopter rises from rest on the ground vertically upwards with a constant acceleration g. A food packet is dropped from the helicopter when it is at a height $h$. The time taken by the packet to reach the ground is close to [ g is the acceleration due to gravity] :
(1) $t=3.4 \sqrt{\left(\frac{h}{g}\right)}$
(2) $t=\sqrt{\frac{2 h}{3 g}}$
(3) $t=\frac{2}{3} \sqrt{\left(\frac{h}{g}\right)}$
(4) $t=1.8 \sqrt{\frac{h}{g}}$

Sol. 1

$V_{B}{ }^{2}=0^{2}+2 g h$
$V_{B}=\sqrt{2 g h}$
$-h=\left(V_{B}\right) t-\frac{1}{2} g t^{2}$
$-h=\sqrt{2 g h t}-\frac{1}{2} g t^{2}$
$g t^{2}-2 \sqrt{2 g h t}-2 h=0$
$\mathrm{t}=\frac{\sqrt{2 \mathrm{ght}} \pm \sqrt{8 \mathrm{gh}+8 \mathrm{gh}}}{2 \mathrm{~g}}=\frac{2 \sqrt{2 \mathrm{gh}} \pm \sqrt{16} \mathrm{gh}}{2 \mathrm{~g}}=\frac{\sqrt{2 g h}+2 \sqrt{\mathrm{gh}}}{\mathrm{g}}$
$t=\sqrt{\frac{2 h}{g}}+2 \sqrt{\frac{h}{g}}=\sqrt{\frac{h}{g}}(\sqrt{2}+2)=3.4 \sqrt{\frac{h}{g}}$
7. A bullet of mass 5 g , travelling with a speed of $210 \mathrm{~m} / \mathrm{s}$, strikes a fixed wooden target. One half of its kinetic energy is converted into heat in the bullet while the other half is converted into heat in the wood. The rise of temperature of the bullet if the specific heat of its material is $0.030 \mathrm{cal} /\left(\mathrm{g}-{ }^{\circ} \mathrm{C}\right)\left(1 \mathrm{cal}=4.2 \times 10^{7} \mathrm{ergs}\right)$ close to :
(1) $38.4^{\circ} \mathrm{C}$
(2) $87.5^{\circ} \mathrm{C}$
(3) $83.3^{\circ} \mathrm{C}$
(4) $119.2^{\circ} \mathrm{C}$

Sol. 2

$$
\left(\frac{1}{2} m v^{2}\right) \times \frac{1}{2}=m s \Delta T \quad s=0.03 \mathrm{cal} / y^{\circ} \mathrm{C}
$$

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$\frac{v^{2}}{4}=126 \times \Delta T$
$v^{2}=4 \times 126 \times \Delta T$
$(210)^{2}=4 \times 126 \times \Delta T$
$210 \times 210=4 \times 126 \times \Delta T$
$44100=504 \times \Delta T$
$\Delta \mathrm{T}=\frac{44100}{504}=87.5^{\circ} \mathrm{C}$
$=\frac{0.03 \times 4.2 \mathrm{~J}}{10^{-3} \mathrm{kgC}}$
$=126 \mathrm{~J} / \mathrm{kgC}$
8. A wheel is rotating freely with an angular speed $\omega$ on a shaft. The moment of inertia of the wheel is I and the moment of inertia of the shaft is negligible. Another wheel of moment of inertia 3I initially at rest is suddenly coupled to the same shaft. The resultant fractional loss in the kinetic energy of the system is :
(1) $\frac{3}{4}$
(2) 0
(3) $\frac{5}{6}$
(4) $\frac{1}{4}$

Sol. 1
$\mathrm{k}_{\mathrm{i}}=\frac{1}{2} \mathrm{I} \omega^{2}$
$k_{f}=\frac{1}{2}(4 \mathrm{I})\left(\omega^{\prime}\right)^{2}$
$=2 \mathrm{I}\left(\frac{\omega}{4}\right)^{2}=\frac{1}{8} \mathrm{I} \omega^{2}$
A.M.C
$\mathrm{I} \omega=(\mathrm{I}+3 \mathrm{I}) \omega^{\prime}$
$\omega^{\prime}=\frac{\mathrm{I} \omega}{4 \mathrm{I}}=\frac{\omega}{4}$
$=\frac{\mathrm{K}_{\mathrm{i}}-\mathrm{K}_{f}}{\mathrm{~K}_{\mathrm{i}}} \Rightarrow \frac{\frac{1}{2} \mathrm{I} \omega^{2}-\frac{1}{8} \mathrm{I} \omega^{2}}{\frac{1}{2} \mathrm{I} \omega^{2}}$
$\frac{\frac{3}{8} \mathrm{I} \omega^{2}}{\frac{1}{2} \mathrm{I} \omega^{2}}=\frac{3}{4}$

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9. A balloon is moving up in air vertically above a point $A$ on the ground. When it is at a height $h_{1}$, $a$ girl standing at a distance $d$ (point $B$ ) from $A$ (see figure) sees it at an angle $45^{\circ}$ with respect to the vertical. When the balloon climbs up a further height $h_{2}$, it is seen at an angle $60^{\circ}$ with respect to the vertical if the girl moves further by a distance 2.464 d (point C). Then the height $h_{2}$ is (given $\tan 30^{\circ}=0.5774$ ) :

(1) 0.464 d
(2) d
(3) 0.732 d
(4) 1.464 d

Sol. 2
$\triangle \mathrm{ABD}$
$\tan 45=\frac{\mathrm{h}_{1}}{\mathrm{~d}}$
$\Rightarrow 1=\frac{\mathrm{h}_{1}}{\mathrm{~d}} \Rightarrow \mathrm{~h}_{1}=\mathrm{d}$
$\triangle \mathrm{ACE}$
$\tan 30=\frac{h_{1}+h_{2}}{d+2.464 d}$
$0.5774=\frac{d+h_{2}}{3.464 d}$
$d+h_{2}=0.5774 \times 3.464 \times d$
$h_{2}=2.0001136 d-d$
$h_{2}=2.000 d-d=d$


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10. An electrical power line, having a total resistance of $2 \Omega$, delivers 1 kW at 220 V . The efficiency of the transmission line is approximately :
(1) $72 \%$
(2) $91 \%$
(3) $85 \%$
(4) $96 \%$

Sol. 4
$\eta=\frac{P_{\text {out }}}{\left(P_{\text {out }}+P_{\text {loss }}\right)} \times 100$
$I=\frac{P}{V}$
$=\frac{100}{220}=\frac{5}{11} \mathrm{~A}$
$P_{\text {loss }}=I^{2} R$
$=\left(\frac{50}{11}\right)^{2} \times 2=41.322$
$\eta=\frac{1000}{1000+41.322} \times 100$
$\eta=96 \%$
11. Activities of three radioactive substances $A, B$ and $C$ are represented by the curves $A, B$ and $C$, in the figure. Then their half-lives $\mathrm{T}_{\frac{1}{2}}(A): \mathrm{T}_{\frac{1}{2}}(B): \mathrm{T}_{\frac{1}{2}}(C)$ are in the ratio:

(1) $3: 2: 1$
(2) $2: 1: 1$
(3) $4: 3: 1$
(4) $2: 1: 3$

Sol. 4
$R_{A}=R_{0} A e^{-\frac{\ln 2}{T}(t)}$
$\ln \left(R_{A}\right)=\ln \left(R_{0} A\right)-\lambda t$
( $\lambda=$ slope of graph $)$
$\lambda_{\mathrm{A}}=\frac{6}{10}=\frac{\ln 2}{\mathrm{~T}_{\mathrm{A}}}$
$\lambda_{B}=\frac{6}{5}=\frac{\ln 2}{T_{B}}$
$\lambda_{\mathrm{C}}=\frac{2}{5}=\frac{\ln 2}{\mathrm{~T}_{\mathrm{C}}}$


## हमारा विश्वास... हू एक विद्यार्यी है खुास

$\left.\begin{array}{l}T_{A}=\frac{5}{3} \ln 2 \\ \mathrm{I}_{\mathrm{B}}=\frac{5}{6} \ln 2\end{array}\right\} \Rightarrow \mathrm{T}_{\mathrm{A}}: \mathrm{T}_{\mathrm{B}}: \mathrm{T}_{\mathrm{C}}=\frac{1}{3}: \frac{1}{6}: \frac{1}{2}$
$\mathrm{T}_{\mathrm{C}}=\frac{5}{2} \ln 2$
$=2: 1: 3$
12. The value of the acceleration due to gravity is $g_{1}$ at a height $h=\frac{R}{2}$ ( $R=$ radius of the earth) from the surface of the earth. It is again equal to $g_{1}$ at a depth $d$ below the surface of the earth. The ratio $\left(\frac{d}{R}\right)$ equals :
(1) $\frac{4}{9}$
(2) $\frac{1}{3}$
(3) $\frac{5}{9}$
(4) $\frac{7}{9}$

Sol. 3
$\mathrm{g}_{\text {at high }}=\mathrm{g}_{\text {at depth }}$
$g_{\text {surface }}=\frac{G M}{R^{2}}$
$\mathrm{g}\left(1-\frac{\mathrm{d}}{\mathrm{R}}\right)=\frac{\mathrm{GMe}}{(\mathrm{R}+\mathrm{h})^{2}}$
$g\left(1-\frac{d}{R}\right)=\frac{G M}{R^{2}\left(1+\frac{h}{R}\right)^{2}}=\frac{g}{\left(1+\frac{R}{2 R}\right)^{2}}=\frac{4 g}{9}$
$\frac{d}{R}=1-\frac{4}{9}=\frac{5}{9}$
13. A hollow spherical shell at outer radius $R$ floats just submerged under the water surface. The inner radius of the shell is $r$. If the specific gravity of the shell material is $\frac{27}{8} w . r . t$ water, the value of $r$ is:
(1) $\frac{4}{9} R$
(2) $\frac{8}{9} R$
(3) $\frac{1}{3} R$
(4) $\frac{2}{3} R$

Sol. 2
$F_{B}=m g$
$\rho_{\ell} V_{\text {body }} g$ (displaced water)

$$
\begin{aligned}
& =\quad \rho_{\mathrm{b}} \mathrm{~V}_{\mathrm{b}} \mathrm{~g} \\
& \text { where mater } \\
& \text { present }
\end{aligned}
$$

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$$
\begin{aligned}
& \frac{4}{3} \pi R^{3}=\frac{\rho_{b}}{\rho_{\ell}}\left(\frac{4}{3} \pi R^{3}-\frac{4}{3} \pi r^{3}\right) \\
& R^{3}=\frac{27}{8}\left(R^{3}-r^{3}\right) \\
& \frac{8}{27} R^{3}=R^{3}-r^{3} \Rightarrow r^{3}=R^{3}-\frac{8 R^{3}}{27}=\frac{19}{27} R^{3} \\
& r=\frac{(19)^{1 / 3}}{3} R \approx 0.88 \approx \frac{8}{9} R
\end{aligned}
$$


14. In a resonance tube experiment when the tube is filled with water up to a height of 17.0 cm from bottom, it resonates with a given tuning fork. When the water level is raised the next resonance with the same tuning fork occurs at a height of 24.5 cm . If the velocity of sound in air is $330 \mathrm{~m} / \mathrm{s}$, the tuning fork frequency is :
(1) 2200 Hz
(2) 550 Hz
(3) 3300 Hz
(4) 1100 Hz

Sol. 1

$\ell_{1}=\ell-17$
$\ell_{2}=\ell-24.5$
$v=2 f\left(\ell_{1}-\ell_{2}\right)$
$330=2 \times \mathrm{f} \times\left[\left(\mathrm{f} \times[(\ell-17)-(\ell-24.5)] \times 10^{-2}\right.\right.$
$165=\mathrm{f} \times 7.5 \times 10^{-2}$
$\mathrm{f}=\frac{165 \times 1000}{7.5}$
$\mathrm{f}=2200 \mathrm{~Hz}$
15. A solid sphere of radius $R$ carries a charge $Q+q$ distributed uniformly over its volume. A very small point like piece of it of mass $m$ gets detached from the bottom of the sphere and falls down vertically under gravity. This piece carries charge $q$. If it acquires a speed $v$ when it has fallen through a vertical height y (see figure), then : (assume the remaining portion to be spherical).

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(1) $v^{2}=2 y\left[\frac{q Q}{4 \pi \in_{0} R(R+y) m}+g\right]$
(2) $v^{2}=2 y\left[\frac{\mathrm{QqR}}{4 \pi \epsilon_{0}(\mathrm{R}+\mathrm{y})^{3} \mathrm{~m}}+\mathrm{g}\right]$
(3) $v^{2}=y\left[\frac{q Q}{4 \pi \in_{0} R(R+y) m}+g\right]$
(4) $v^{2}=y\left[\frac{q Q}{4 \pi \in_{0} R^{2} y m}+g\right]$

Sol. 1
M.E.C.
$K_{A}+U_{A}=K_{B}+U_{B}$
$0+m g y+\mathrm{qV}_{\mathrm{A}}=\frac{1}{2} m v^{2}+0+\left(+\mathrm{qv}_{\mathrm{B}}\right)$
$m g y+\mathrm{qV}_{\mathrm{A}}=\frac{1}{2} m v^{2}+q\left(\mathrm{~V}_{\mathrm{B}}\right)$
$m g y+\frac{q k(Q)}{R}=\frac{1}{2} m v^{2}+\frac{q k(Q)}{R+y}$
$\frac{1}{2} m v^{2}=-\frac{k q(Q)}{R+y}+\frac{k q(Q)}{R}+m g y$
$\frac{m v^{2}}{2}=\frac{-k q(Q) R+k q(Q)(R+y)}{R(R+y)}+m g y$
$v^{2}=\frac{2}{m}\left[\frac{-k q Q R+k q Q R+k q Q}{R(R+y)}+m g y\right]$
$v^{2}=\frac{2}{m}\left[\frac{k q(Q) y}{R(R+y)}+m g y\right]$

potential at A
$V_{A}=\frac{k(Q+q)}{R}$
$v^{2}=2 y\left[\frac{q(Q)}{4 \pi \varepsilon_{0} R(R+y) m}+g\right]=2 y\left[\frac{q Q}{4 \pi \varepsilon_{0} R(R+y) m}+g\right] \quad v_{B}=\frac{k(Q+q)}{R+y}$

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16. A galvanometer of resistance $G$ is converted into a voltmeter of range $0-1 \mathrm{~V}$ by connecting a resistance $R_{1}$ in series with it. The additional resistance that should be connected in series with $R_{1}$ to increase the range of the voltmeter to $0-2 \mathrm{~V}$ will be :
(1) G
(2) $R_{1}$
(3) $R_{1}-G$
(4) $R_{1}+G$

Sol. 4
$V=I\left(R_{1}+G\right)$
$\frac{1}{2}=\frac{I\left(R_{1}+G\right) \ldots .(i)}{I\left(R_{1}+R_{2}+G\right) \ldots .(i i)}$

$\frac{1}{2}=\frac{R_{1}+G}{R_{1}+R_{2}+G}$
$R_{1}+R_{2}+G=2 R_{1}+2 G$
$R_{2}=R_{1}+G$

17. Number of molecules in a volume of $4 \mathrm{~cm}^{3}$ of a perfect monoatomic gas at some temperature $T$ and at a pressure of 2 cm of mercury is close to ? (Given, mean kinetic energy of a molecule (at T ) is 4 $\times 10^{-14} \mathrm{erg}, \mathrm{g}=980 \mathrm{~cm} / \mathrm{s}^{2}$, density of mercury $=13.6 \mathrm{~g} / \mathrm{cm}^{3}$ )
(1) $4.0 \times 10^{18}$
(2) $4.0 \times 10^{6}$
(3) $5.8 \times 10^{16}$
(4) $5.8 \times 10^{18}$

Sol. 1
$\mathrm{KE}=\frac{3}{2} \mathrm{kT} \Rightarrow\left(\mathrm{T}=\frac{2 \mathrm{E}}{3 \mathrm{k}}\right), \mathrm{PV}=\mathrm{NkT}$
$P=\rho g h, V=4 \mathrm{~cm}^{3}$
$13.6 \times 10^{3} \times 9.8 \times 2 \times 10^{-2} \times 4 \times 10^{-6}$
$=\mathrm{Nk} \times \frac{2 \mathrm{E}}{3 \mathrm{k}}=\frac{\mathrm{N} \times 2}{3} \times 4 \times 10^{-14} \times 10^{7}$
$N=\frac{13.6 \times 19.6 \times 4 \times 10^{-5} \times 3 \times 10}{8}$
$N=399.84 \times 10^{16}$
$=3.99 \times 10^{18}$
$\mathrm{N}=4 \times 10^{18}$
18. An electron is constrained to move along the $y$-axis with a speed of 0.1 c (c is the speed of light) in the presence of electromagnetic wave, whose electric field is $\vec{E}=30 \hat{j} \sin \left(1.5 \times 10^{7} t-5 \times 10^{-2} x\right)$ $\mathrm{V} / \mathrm{m}$. The maximum magnetic force experienced by the electron will be :
(given $\mathrm{c}=3 \times 10^{8} \mathrm{~ms}^{-1}$ and electron charge $=1.6 \times 10^{-19} \mathrm{C}$ )
(1) $2.4 \times 10^{-18} \mathrm{~N}$
(2) $4.8 \times 10^{-19} \mathrm{~N}$
(3) $3.2 \times 10^{-18} \mathrm{~N}$
(4) $1.6 \times 10^{-19} \mathrm{~N}$

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Sol. 2
$v_{e}=0.1 C$ along $y$-axis direction of emwave - along $(x)$
$\vec{E}=\vec{V} \times \vec{B}$
$E=C B \Rightarrow B=E / C$
$\therefore$ force on $\mathrm{e}^{-}$will be max.
If $B$ is $\perp$ to $y$-along $z$-axis
[ $\because \mathrm{E}$ also $\perp \mathrm{B}, \mathrm{B}$ also $\perp$ to direction of motion of wave]
$\therefore \mathrm{B} \rightarrow$ along $\mathrm{Bz}(-\mathrm{z})$ as
$B=\frac{30}{C} \sin \left(1.5 \times 10^{7} t-5 \times 10^{-2} x\right)$

$\mathrm{B}_{\text {max }}=\frac{30}{3 \times 10^{8}}=10^{-7} \mathrm{~T}$
$\theta=90$ between $v_{e} \& B$ so $F_{\max }=q v B$
$F_{\max }=\mathrm{e} \times(0.1 \times C) \times \frac{30}{C}$
$=1.6 \times 10^{-19} \times 3$
$F_{\max }=4.8 \times 10^{-19} \mathrm{~N}$
19. For a concave lens of focal length $f$, the relation between object and image distances $u$ and $v$, respectively, from its pole can best be represented by ( $u=v$ is the reference line) :
(1)

(2)

(3)

(4)


Sol. 4
Concave lens graph u v/s v by u-v graph theory

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20. A physical quantity $z$ depends on four observables $a, b, c$ and $d$, as $z=\frac{a^{2} b^{\frac{2}{3}}}{\sqrt{c} d^{3}}$. The percentages of error in the measurement of $a, b, c$ and $d$ are $2 \%, 1.5 \%, 4 \%$ and $2.5 \%$ respectively. The percentage of error in $z$ is :
(1) $16.5 \%$
(2) $12.25 \%$
(3) $13.5 \%$
(4) $14.5 \%$

Sol. 4
$z=a^{2} b^{2 / 3} c^{-1 / 2} d^{-3}$
$100 \times \frac{\mathrm{dz}}{\mathrm{z}}=\left(2 \frac{\mathrm{da}}{\mathrm{a}}+\frac{2}{3} \frac{\mathrm{db}}{\mathrm{b}}+\frac{1}{2} \frac{\mathrm{dc}}{\mathrm{c}}+3 \frac{\mathrm{~d}(\mathrm{~d})}{(\mathrm{d})}\right) \times 100$
\% error in z
$=\left(2 \times 2+\frac{2}{3} \times 1.5+\frac{1}{2} \times 4+3 \times 2.5\right) \%$
$=4+1+2+7.5$
$=14.5 \%$
21. A particle of mass $200 \mathrm{Me} V / \mathrm{c}^{2}$ collides with a hydrogen atom at rest. Soon after the collision the particle comes to rest, and the atom recoils and goes to its first excited state. The initial kinetic energy of the particle (in eV ) is $\frac{\mathrm{N}}{4}$. The value of N is :
(Given the mass of the hydrogen atom to be $1 \mathrm{GeV} / \mathrm{c}^{2}$ ) $\qquad$ _.
Sol. 51
$\mathrm{m}_{\mathrm{H}}=1 \mathrm{GeVC}^{2}=1000 \mathrm{MeV} / \mathrm{C}^{2}, \mathrm{~m}_{\text {particle }}=200 \mathrm{meV} / \mathrm{c}^{2}=\mathrm{m}$

$\therefore \mathrm{mv}_{0}+0=0+5 \mathrm{mV}^{\prime} \Rightarrow \mathrm{v}^{\prime}=\frac{\mathrm{v}_{0}}{5}$

## हमारा विश्वास... हर एक विद्यार्थी है ख़ास

loss in KE
$=\frac{1}{2} m v_{0}{ }^{2}-\frac{1}{2}(5 \mathrm{~m})\left(\frac{\mathrm{v}_{0}}{5}\right)^{2}$
$=\frac{4}{5}\left(\frac{m v_{0}^{2}}{2}\right)=\frac{4}{5} \mathrm{k}$
$\frac{4}{5} \mathrm{k}=10.2$
$k=12.75 \mathrm{eV}=\frac{12.75}{100}=\frac{51}{4}$
so $=\mathrm{n}=51$
22. Two concentric circular coils, $C_{1}$ and $C_{2}$, are placed in the $X Y$ plane. $C_{1}$ has 500 turns, and a radius of $1 \mathrm{~cm} . \mathrm{C}_{2}$ has 200 turns and radius of $20 \mathrm{~cm} . \mathrm{C}_{2}$ carries a time dependent current $I(t)=\left(5 t^{2}-2 t+3\right) A$ where $t$ is in $s$. The emf induced in $C_{1}$ (in $\left.m V\right)$, at the instant $t=1$ is $\frac{4}{x}$. The value of $x$ is $\qquad$ .

Sol. 5
$B_{2}=\frac{\mu_{0} I_{2} N_{2}}{2 R_{2}}$
$\phi=N_{1} B_{2} \pi R_{1}^{2}=N_{1} N_{2} \frac{\mu_{0} \mathrm{I}}{2 \mathrm{R}_{2}} \pi \mathrm{R}_{1}{ }^{2}$
$e=\frac{d \phi}{d t}$
$\phi=\frac{500 \times 200 \times 4 \pi \times 10^{-7} \times\left(5 \mathrm{t}^{2}-2 \mathrm{t}-3\right) \pi\left(10^{-2}\right)^{2}}{2 \times 20 \times 10^{-2}}$
$\frac{10^{5} \times 4 \pi^{2} \times 10^{-7}\left(5 t^{2}-2 t+3\right) \times 10^{-4}}{40 \times 10^{-2}}$
$\phi=\left(5 t^{2}-2 t+3\right) \times 10^{-4}$
$e=\left|\frac{d \phi}{d t}\right|=(10 t-2) \times 10^{-4}$
$\mathrm{t}=1 \mathrm{sec}$
$e=8 \times 10^{-4}=0.8 \mathrm{mV}=\frac{0.8}{10}=\frac{4}{5}$
$x=5$

हमारा विश्वास... हर एक विद्यार्थी है ख़ास
23. A beam of electrons of energy $E$ scatters from a target having atomic spacing of $1 \AA$. The first maximum intensity occurs at $\theta=60^{\circ}$ Then $E$ (in eV) is $\qquad$ .
(Planck constant $\mathrm{h}=6.64 \times 10^{-34} \mathrm{Js}, 1 \mathrm{eV}=1.6 \times 10^{-19} \mathrm{~J}$, electron mass $\mathrm{m}=9.1 \times 10^{-31} \mathrm{~kg}$ )
Sol. 5
$2 \mathrm{~d} \sin \theta=\mathrm{n} \lambda=1 \times \sqrt{\frac{150}{\mathrm{v}} \times 10^{-10}}, \theta=90-\frac{\phi}{2}$
$2 \times 10^{-10} \times \sin 60=\sqrt{\frac{150}{\mathrm{~V}}} \times 10^{-10}, \theta=90-\frac{60}{2}=60$
$2 \times \frac{\sqrt{3}}{2}=\sqrt{\frac{150}{V}}$
$V=\frac{150}{3}=50$ volt
$E=e v=50 \mathrm{ev}$
24. A compound microscope consists of an objective lens of focal length 1 cm and an eye piece of focal length 5 cm with a separation of 10 cm . The distance between an object and the objective lens, at which the strain on the eye is minimum is $\frac{n}{40} \mathrm{~cm}$. The value of $n$ is $\qquad$ .
Sol. 50

$\mathrm{f}_{0}=1 \mathrm{~cm}, \mathrm{f}_{\mathrm{e}}=5 \mathrm{~cm}, \mathrm{u}_{0}=$ ?
final image at ( $\infty$ )
( $\mathrm{v}_{\mathrm{e}}=\infty$ )
$v_{0}+u_{e}=10 \mathrm{~cm}$
$v_{0}+5=10$
$\mathrm{L}=\mathrm{v}_{\mathrm{o}}+\mathrm{u}_{\mathrm{e}}=10 \mathrm{~cm}$
$\frac{1}{v_{e}}-\frac{1}{u_{e}}=\frac{1}{f_{e}}$
$\mathrm{v}_{0}=5 \mathrm{~cm}$
$\frac{1}{\infty}-\frac{1}{u_{e}}=\frac{1}{5}$
$\frac{1}{\mathrm{v}_{0}}-\frac{1}{\mathrm{u}_{0}}=\frac{1}{\mathrm{f}_{0}}$
$u_{e}=-5 c m$
$\frac{1}{5}-\frac{1}{u_{0}}=\frac{1}{1}$
$\left|u_{e}\right|=5$

## हमारा विश्वास... हू एक विद्यार्यी है खुास

$\frac{1}{u_{0}}=\frac{1}{5}-1=-\frac{4}{5} \Rightarrow u_{0}=-\frac{4}{5}$
$\left|u_{0}\right|=\frac{5}{4}=\frac{50}{40}=\frac{n}{40}$
$\therefore \mathrm{n}=50$
25. $A$ force $\vec{F}=(\hat{i}+2 \hat{j}+3 \hat{k}) N$ acts at a point $(4 \hat{i}+3 \hat{j}-\hat{k}) \mathrm{m}$. Then the magnitude of torque about the point $(\hat{i}+2 \hat{j}+\hat{k}) m$ will be $\sqrt{x} N-m$. The value of $x$ is $\qquad$ .

## Sol. 195

$\vec{\tau}=\vec{r} \times F=(3 \hat{i}+\hat{j}-2 \hat{k}) \times(\hat{i}+2 \hat{j}+3 \hat{k})$
$=\left|\begin{array}{ccc}i & j & k \\ 3 & 1 & -2 \\ 1 & 2 & 3\end{array}\right|$
$\hat{i}(3+4)-\hat{j}(9+2)+\hat{k}(6-1)$
$\vec{\tau}=7 \hat{j}-11 \hat{j}+5 \hat{k}$
$|\vec{\tau}|=\sqrt{49+121+25}=\sqrt{195}$
$x=195$

# जब इन्हीने पूरा किया अपना सपना तो आप भी पा सकते है लेक्ष्य अपना 

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